

Solutions of the test Unit-2 paper-1, held on 11-01-2010

Chemistry :

1. Ans. : A

Sol. Enthalpy change is constant for strong acid and strong base neutralization.

2. Ans. : B

Sol. $Q = 500 \times 20 \times 4.18 \text{ J}$

No. of ice cubes = $Q / 6.02 \times 1000 = 7$

3. Ans. : A

Sol. after 15 min concentration of A = $4B / 8 = B/2$

after 15 min concentration of B = $B/2$

4. Ans. : B

Sol. $\Delta C = \Delta P/RT = 0.8 / 0.082 \times 298 = 0.0327 \text{ mole/L}$

Rate = $\Delta C / t = 0.032 / 3000 = 1.09 \times 10^{-5}$

5. Ans. : A

6. Ans. : C

Sol. for Ag_2CrO_4 : $[\text{Ag}^+] = 2s$ where $s = \sqrt[3]{\frac{K_{sp}}{4}}$; $[\text{Ag}^+] =$

7. Ans. : B

8. Ans. : D

Sol. use conductance = conductivity / cell constant ; $y = x / G$;

$z = K / G$; $K = z x / y$;

$$\lambda_m = \frac{K \times 1000}{C} = \frac{z \cdot \frac{x}{y} \times 1000}{0.1}$$

9. Ans. : B, C,

Sol. $[\text{B}] : [\text{C}] : [\text{D}] = 2 k_1 : k_2 : 3 k_3$

$1/k = 1/k_1 + 1/k_2 + 1/k_3$; $t_{1/2} = 0.693/k = 198 \text{ sec}$

$[\text{A}_0] = [\text{A}] + [\text{B}]/2 + [\text{C}] + [\text{D}]/3$

10. Ans. : ABCD

11. Ans. : B,C

Sol. for $\Delta H = \Delta E$; $\Delta n = 0$

12. Ans. : AB

Sol. The metals deposited at the cathode must have positive reduction potential

13. Ans. : B

14. Ans. ; D

Sol. solution is acidic so , $E_0 = 1.229 - (-0.447) = 1.676 \text{ V}$

15. Ans. : D

16. Ans.. B

17. Ans. : D

18. Ans. : A

19. A – R, B – S, C – P, D – Q

20. A – PRS; B – QT; C – QT, D – PRS

MATHEMATICS

21. Ans. : B

Sol. Let S be the given focus and ZM be the given line.

$$\begin{aligned} \text{Then } SZ &= a/e - ae. \\ &= a/e (1 - e^2) = b^2/ae = k \text{ (say)} \\ \text{as } b^2 &= a^2(1 - e^2) \end{aligned}$$

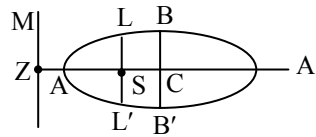
Now, take SC as x-axis and LSL as y-axis.

Let (x, y) be the co-ordinates of B w.r.t. these axes.

$$\text{Then } x = SC = ae, y = CB = b.$$

Hence $y^2/x = b^2/ae = SZ$, which is constant.

$\therefore y^2 = kx$ is the required locus which is a parabola.



22. Ans. : B

Sol. The normal to an ellipse at P must pass through the centre (3, 0) of the circle is

$$\begin{aligned} \frac{ax}{\cos \theta} - \frac{by}{\sin \theta} &= a^2 - b^2 \\ \rightarrow \frac{5x}{\cos \theta} - \frac{4y}{\sin \theta} &= 9 \quad \left[\because \theta = 0 \text{ or } \frac{\pi}{2} \right] \end{aligned}$$

$$\rightarrow \frac{15}{\cos \theta} - 0 = 9 \rightarrow \cos \theta = \frac{15}{9}$$

\rightarrow Which is not possible.

$$\rightarrow \theta = 0 \text{ or } \pi/2$$

$$\text{But } \theta \neq \pi/2 \rightarrow \theta = 0$$

Hence, p \equiv (5, 0) i.e., end of major axis.

23. Ans. : C

Sol. We have, $\sqrt{px} + \sqrt{qy} = 1$

$$\rightarrow (\sqrt{px} + \sqrt{qy})^2 = 1$$

$$\rightarrow px + qy + 2\sqrt{pqxy} = 1$$

$$\rightarrow (px + qy - 1)^2 = 4pqxy$$

$$\rightarrow p^2x^2 - 2pqxy + q^2y^2 - 2px - 2qy + 1 = 0$$

On comparing this equation with the equation

$$ax^2 + 2hxy + by^2 + 2gx + 2fy + c = 0$$

We get $a = p^2$, $b = q^2$, $c = 1$, $g = -p$, $f = -q$ and $h = -pq$.

$$\begin{aligned} \therefore \Delta &= abc + 2fgh - af^2 - bg^2 - ch^2 \\ &= p^2q^2 - 2p^2q^2 - p^2q^2 - p^2q^2 - p^2q^2 \\ &= -4p^2q^2 \neq 0 \text{ and } b^2 - ab = p^2q^2 - p^2q^2 = 0 \end{aligned}$$

Thus, we have $\Delta \neq 0$ and $h^2 = ab$.

So the given equation represents a parabola.

24. Ans. : D

Sol. Let the coordinates of P be (α, β)

$$\text{Then, } PQ = 2\beta \quad OP = \sqrt{\alpha^2 + \beta^2}$$

Since, OPQ is an equilateral triangle $OP = PQ$

$$\rightarrow \alpha^2 + \beta^2 = 4\beta^2 \rightarrow \alpha^2 = 3\beta^2$$

$$\rightarrow \alpha = \pm \sqrt{3\beta}$$

Also, since (α, β) lies on the given hyperbola

$$\frac{\alpha^2}{a^2} - \frac{\beta^2}{b^2} = 1$$

$$\rightarrow \frac{3\beta^2}{a^2} - \frac{\beta^2}{b^2} = 1 \rightarrow \frac{3}{a^2} - \frac{1}{b^2} = \frac{1}{\beta^2} > 0 = \frac{b^2}{a^2} > \frac{1}{3}$$

$$e^2 - 1 > 1/3 \rightarrow e^2 > 4/3 \rightarrow e > \frac{2}{\sqrt{3}}.$$

25. Ans. C

Sol. Equation of the normal of the parabola $y^2 = 4ax$ with slope m is

$$y = mx - 2am - am^2$$

It touches $x^2 - y^2 = a^2$ if

$$(-2am - am^3)^2 = a^2m^2 - a^2.$$

$$\left[\because y = mx + c \text{ touches } \frac{x^2}{a^2} - \frac{y^2}{b^2} = 1 \text{ if } c^2 = a^2 m^2 - b^2 \right]$$

$$\rightarrow a^2 m^2 (2 + m^2)^2 = a^2 (m^2 - 1)$$

$$\rightarrow m^2 (m^4 + 4m^2 + 4) = m^2 - 1$$

$$\rightarrow m^6 + 4m^4 + 3m^2 + 1 = 0$$

26. Ans. : C

Sol. Any tangent to the parabola $y^2 = 4ax$ is $y = mx + \frac{1}{m}$ (1)

It is a tangent to the circle $(x - 3)^2 + y^2 = 9$ if the length of the \perp from the centre $(3, 0)$ upon (1) is equal to radius of the circle i.e., 3.

$$\therefore \frac{\left| 3m + \frac{1}{m} - 0 \right|}{\sqrt{1+m^2}} = 3$$

$$\rightarrow am^2 + \frac{1}{m^2} + 6 = 9(1 + m^2) = 9 + 9m^2$$

$$\rightarrow \frac{1}{m^2} + 6 = 9 \rightarrow \frac{1}{m^2} = 3 \quad \therefore m^2 = \frac{1}{3}$$

$$\rightarrow m = \pm \frac{1}{\sqrt{3}} \quad \text{But } m > 0$$

[\because Parabola is above x-axis]

$$\therefore \text{required line is } y = \frac{1}{\sqrt{3}}x + \sqrt{3} \rightarrow \sqrt{3}y = x + 3$$

27. Ans. : A

Sol. Take A as origin and AB, AC as x-axis, y-axis respectively.

Let AB = a, AC = b

\therefore B is (a, 0), C is (0, b). Since BC \parallel PQ

$$\therefore \frac{AP}{AB} = \frac{AQ}{AC} = k$$

$$\therefore AP = KAB = Ka$$

$$AQ = KAC = Kb$$

$$\text{Equation of BQ is } \frac{x}{a} + \frac{y}{b} = 1 \quad \dots\dots (1)$$

$$\text{Equation of PC is } \frac{x}{Ka} + \frac{y}{b} = 1 \quad \dots\dots (2)$$

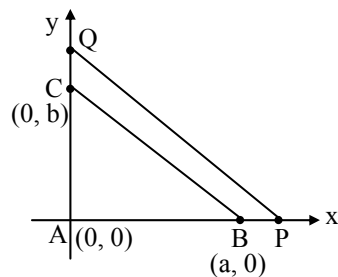
(1) - (2) gives

$$\frac{x}{a} \left(1 - \frac{1}{K} \right) + \frac{y}{b} \left(\frac{1}{K} - 1 \right) = 0$$

$$\rightarrow \frac{x}{a} - \frac{y}{b} = 0 \rightarrow bx - ay = 0$$

Which is a straight line passing through A(0, 0).

This is required locus.



28. Ans. : B

Sol. Let B be (x, y) and the C be (4, y). Since medians through B and C meet at (4, 1)

\therefore centroid G of ΔABC is (4, 1)

$$\therefore \frac{x_1 + 4 + 1}{3} = 4 \rightarrow x_1 = 7$$

Since B(x₁, y₁) lies on $x + y = 5$

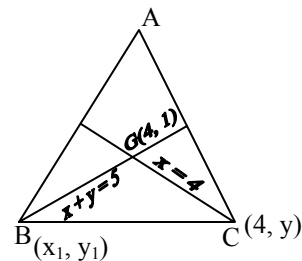
$$\therefore y_1 = 5 - x_1 = 5 - 7 = -2.$$

\therefore B is (7, -2).

$$\text{Also } \frac{y_1 + y + 2}{3} = 1 \rightarrow y = 3 - 1 - y$$

$$= 3 - 2 + 2 = 3$$

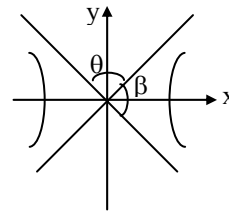
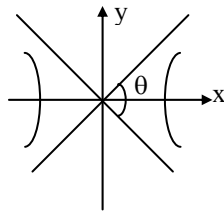
\therefore C is (4, 3)



29. Ans. : AC

Sol. $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1.$

$$\therefore \cos \frac{\theta}{2} = \frac{a}{\sqrt{a^2 + b^2}} = \frac{a}{\sqrt{a^2 e^2}} = \frac{1}{e}$$



$$\therefore \cos \frac{\theta}{2} = \sin \frac{\beta}{2} = \frac{\sqrt{e^2 - 1}}{e}$$

30. Ans. : BD

Sol. Let the line $\lambda x - y + 1 = 0$ intersect the x-axis at A and y-axis at B.

$$\therefore \frac{\text{At A}}{A\left(\frac{1}{\lambda}, 0\right)} \frac{\text{At B}}{(0, 1)}$$

Now let $x - 2y + 3 = 0$ intersect the x-axis at C and y-axis at D

$$\frac{\text{At C}}{C(-3, 0)} \frac{\text{At D}}{(0, 3/2)}$$

$$OA = 1/\lambda$$

$$OC = -3 \quad \frac{3}{2} - \frac{3}{\lambda} = 0$$

$$OB = 1 \quad \lambda = 2$$

$$OD = 3/2.$$

31. Ans. : ABC

Sol. Clearly O is the mid point of SS' and HH'

→ diagonals of quadrilateral HSH'S' bisect each other so it is a parallelogram.

Let H'O/HH' = 2r → OH = r = ae₂

H lies on $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ (suppose)

$$\therefore \frac{r^2 \cos^2 \theta}{a^2} + \frac{r^2 \sin^2 \theta}{b^2} = 1$$

$$e_2^2 \cos^2 \theta + \frac{e_2^2 \sin^2 \theta}{1 - e_1^2} = 1 \quad (\because b^2 = a^2(1 - e_1^2))$$

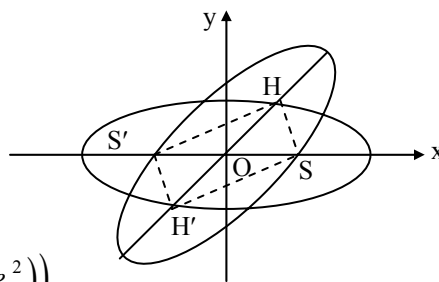
$$\rightarrow e_2^2 \cos^2 \theta + \frac{e_2^2 \cos^2 \theta}{1 - e_1^2} = 1 - \frac{e_2^2}{1 - e_1^2}$$

$$\rightarrow \cos^2 \theta = \frac{1}{e_1^2} + \frac{1}{e_2^2} - \frac{1}{e_1^2 e_2^2}$$

$$\rightarrow \cos \theta = \sqrt{\frac{1}{e_1^2} + \frac{1}{e_2^2} - \frac{1}{e_1^2 e_2^2}}$$

Now, if $e_1^2 + e_2^2 = 1$ (given) so, from eqn. (1) $\cos \theta = 0$

$$\rightarrow \theta = 90^\circ.$$



32. Ans. : ABC

Sol. $PS + PS' = e PZ + e PZ'$

$$= e(ZZ') = e \cdot 2a/e$$

$$= 2a \text{ if } a > b.$$

$$= 2b \text{ if } a < b$$

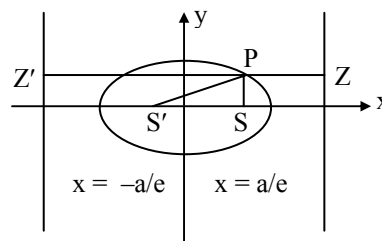
$$PS + PS' + SS' = 2a + 2ae = 2a(1 + e)$$

Semi-perimeter of $\Delta PSS'$, $S = a(1 + e)$

$$\tan \frac{\alpha}{2} \tan \frac{\beta}{2} = \frac{\sqrt{(S - c_1)(S - a_1)(S - a_1)(S - b_1)}}{S(S - b_1)S(S - c_1)} = \frac{S - a_1}{S}$$

$$\text{Now } S - a_1 = SS' = a(1 + e) - 2ac = a(1 - e)$$

$$\therefore \tan \frac{\alpha}{2} \tan \frac{\beta}{2} = \frac{1 - e}{1 + e}$$



33. Ans. A

Sol. $\tan^2 \theta_1 + \tan^2 \theta_2 = k \rightarrow m_1 + m_2^2 = k$

$$(m_1 + m_2)^2 - 2m_1m_2 = k.$$

34. Ans. : C

Sol. $\frac{1}{\tan \theta_1} + \frac{1}{\tan \theta_2} = k \rightarrow \frac{m_2 + m_1}{m_1 m_2} = k$

35. Ans. : A

Sol. $\theta_1 - \theta_2 = \alpha \rightarrow \frac{\tan \theta_1 - \tan \theta_2}{1 + \tan \theta_1 \tan \theta_2} = \tan \alpha$

$$\rightarrow m_1 - m_2 = (1 + m_1 m_2) \tan \alpha$$

$$\rightarrow (m_1 - m_2)^2 = (1 + m_1 m_2)^2 \tan^2 \alpha$$

$$\rightarrow (m_1 + m_2)^2 - 4m_1 m_2 = (1 + m_1 m_2)^2 \tan^2 \alpha.$$

36. Ans. : D

Sol. Let the asymptotes be $2x + 3y + \lambda = 0$ and $3x + 2y + \mu = 0$, it passes through (1, 2)

$$\lambda = -8, \mu = -7$$

$$\text{Equation of hyperbola is } (2x + 3y - 8)(3x + 2y - 7) + \gamma = 0 \quad \dots\dots (1)$$

It passes through (5, 3) $\gamma = -154$.

Putting the value of λ in (1), we get $(2x + 3y - 8)(3x + 2y - 7) - 154 = 0$ is the equation of required hyperbola.

37. Ans. : B

Sol. $2 \tan^{-1} \left(\frac{b}{a} \right) = \frac{\pi}{3} \rightarrow a = b\sqrt{3}$

$$a^2 = b^2(e^2 - 1) \rightarrow e = 2.$$

38. Ans. : C

Sol. $\frac{3x - 4y - 1}{5} = \pm \frac{4x - 3y - 6}{5}$

$$\rightarrow x + y - 5 = 0 \text{ and } x - y - 1 = 0.$$

39. Ans. : A - R, B - Q, C - P, D - S

Sol. $\frac{(x + y - 5)^2}{2} + \frac{(x - y + 7)^2}{3} = 1$

$$\frac{\left(\frac{x + y - 5}{\sqrt{5}} \right)^2}{1} + \frac{\left(\frac{x - y + 7}{\sqrt{2}} \right)^2}{3/2} = 1$$

$x + y - 5 = 0$ is major axis

$x - y + 7 = 0$ is minor axis.

A. $x + y = 5$

$$x - y = -7$$

$$\text{centre} = (-1, 6)$$

B. $1^2 = \frac{3}{2} (1 - e^2)$

$$e = \frac{1}{\sqrt{3}}, ae = \frac{\sqrt{3}}{\sqrt{2}} \cdot \frac{1}{\sqrt{3}} = \frac{1}{\sqrt{2}}$$

Focus $\frac{1}{2}$ distance away from (-1, 6)

$$\left(-1 + \frac{1}{\sqrt{2}} \left(-\frac{1}{\sqrt{2}} \right) \right), \left(6 + \frac{1}{\sqrt{2}} \left(\frac{1}{\sqrt{2}} \right) \right) = \left(-\frac{1}{3}, \frac{13}{2} \right).$$

C. Vertex is $\frac{\sqrt{3}}{2}$ distance away from (-1, 6)

$$= \left(-1 + \frac{\sqrt{3}}{\sqrt{2}} \left(-\frac{1}{\sqrt{2}} \right), 6 + \frac{\sqrt{3}}{\sqrt{2}} \cdot \frac{1}{\sqrt{2}} \right)$$

$$= \left(-1 + \frac{\sqrt{3}}{\sqrt{2}}, 6 + \frac{\sqrt{3}}{\sqrt{2}} \right).$$

D. $\frac{a}{e}$ distance away from centre

$$\begin{aligned} \frac{a}{e} &= \frac{\sqrt{3}}{2} \times \sqrt{3} = \frac{3}{2} \\ &= \left(-1 + \frac{3}{2} \left(-\frac{1}{\sqrt{2}} \right), 6 + \frac{3}{2} \left(\frac{1}{\sqrt{2}} \right) \right) \\ &= \left(-1 - \frac{3}{\sqrt{2}}, 6 + \frac{3}{2\sqrt{2}} \right) \end{aligned}$$

40. Ans. : A – Q, B – P, C – S, D – R

Sol. A. Any tangent of parabola will be of the form $ty = x + at^2$ at the point $(at^2, 2at)$. If this is normal to circle, then this will pass through centre of the circle which is $(a, 2a)$

$$2at = a + at^2$$

$$\rightarrow t^2 - 2t + 1 = 0$$

$\rightarrow t = 1, 1$ for any value of a , so the condition is satisfied for all real values of 'a'.

B. For the point $(k + 3, k)$, the chord of contact $yk - 2x = 2k + 6$

$$\text{Solving with the equation of parabola } \left(\frac{2x + 2k + 6}{k} \right)^2 - 4x$$

$$\rightarrow x^2 + (2k + 6 - k^2)x + (k + 3)^2 = 0$$

$$\rightarrow (2k + 6 - k^2)^2 - 4(k + 3)^2 > 0 \quad (\because D > 0)$$

$$\rightarrow k^2(k - 6)(k + 2) > 0$$

$$\therefore k \in (-\infty, -2) \cup (6, \infty)$$

C. Let the tangents be $y = mx + \frac{1}{m}$ and $(y + \alpha) = m(x - 1) + 4\sqrt{1 + m^2}$

$$\text{Distance between tangent} = \frac{4\sqrt{1 + m^2} - m - 2 - 1/m}{\sqrt{1 + m^2}}$$

$$= 4 - \frac{2}{\sqrt{1 + m^2}} - \frac{\sqrt{m^2 + 1}}{m}$$

$$\text{As } m > 0 \rightarrow \alpha < 4.$$

D. Any tangent to $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ is

$$y = mx \pm \sqrt{a^2 m^2 + b^2} \quad \dots\dots (i)$$

Any tangent to the parabola $y^2 = 4ax$ is

$$y = mx - \frac{a}{m} \quad \dots\dots (ii)$$

Eqs. (i) and (ii) are same line

$$\therefore \sqrt{a^2 m^2 + b^2} = \pm \frac{a}{m}$$

$$\rightarrow a^2 m^2 + b^2 = \frac{a^2}{m^2}$$

$$\rightarrow a^2 \left(\frac{1}{m^2} - m^2 \right) = b^2$$

$$\rightarrow \frac{1}{m^2} - m^2 > 0 \text{ and } \frac{1}{m^2} - m^2 \neq 1$$

$$\rightarrow m \in (-1, 1) - \{0\}, \sqrt{\frac{\sqrt{5} - 1}{2}}$$

PHYSICS – SOLUTIONS

41) D; 42) D; 43) A; 44) A; 45) C; 46) C; 47) A; 48) D; 49) ABC; 50) ABCD; 51) ACD;
 52) ACD; 53) C; 54) A; 55) B; 56) B; 57) D; 58) D; 59) A – Q, B – PR, C – PS, D – PQ;
 60) A – PQ, B – QR, C – PQ, D – PS.

41. Ans. : D

Sol. $\rho = \frac{5NRT_0}{2} \frac{SRT}{M_0}$ As $\rho T = \text{constant}$; $\rho = \text{constant}$.

42. Ans. : D

Sol. $dV = V \gamma dT$ γ, dT are same
 $\therefore dV \propto V$ $\therefore \frac{(dV)_A}{(dV)_B} = \frac{9}{8}$.

43. Ans. A

Sol. $TV^{\gamma-1} = \text{constant}$ $\gamma > 1$ $\therefore \frac{dT}{dV} = -k(\gamma - 1)V^{-\gamma}$

44. Ans. A

Sol. $nc(T_i - T) = \frac{nc(T_i - T_0)}{4}$ $T_i - T = \frac{T_i - T_0}{4}$
 $\ln\left(\frac{T - T_0}{T_i - T_0}\right) = -kt$ $\therefore t = \frac{\ln(4/3)}{k}$

45. Ans. : C

Sol. $Q = nC_v \Delta T = 2P_0V_0$ $\therefore \Delta T = \frac{4T_0}{5}$
 $\therefore T_2 - T_1 = \frac{4T_0}{5}$ $T_2 = \frac{4T_0}{5} + T_0 = \frac{9T_0}{5}$

46. Ans. : C

Sol. $U_3 - U_1 = nC_v(T_3 - T_1) = 3P_0V_0$
 $W_{123} = 3P_0V_0$ $\therefore Q_{123} = 6P_0V_0$

47. Ans. : A

Sol. 1 – 2 is isobaric process $Q_{12} = \frac{7NRT_0}{2}$
 2 – 3 is isochoric process $Q_{23} = \frac{5NRT_0}{2}$
 $\therefore Q_{123} = 6NRT_0$
 $\therefore C = \frac{Q_{123}}{N(3T_0 - T_0)} = 3R$

48. Ans. : D

Sol. $W_{\text{net}} < 0$ $\therefore Q_{\text{cycle}} < 0$.

49. Ans. : ABC

Sol. $U_b - U_a = n\left(\frac{3R}{2}\right)(2T_0 - T_0) = \frac{3nRT_0}{2}$
 V decreases $\therefore W < 0$
 $\rho = \frac{nRT}{V}$. ρ increases.

50. Ans. : ABCD

Sol. $W_{ab} = Q_{ab} = -nRT_0 \ln 2$ $W_{bc} = 0$
 $W_{cd} = Q_{cd} = nR(3T_0) \ln 2$.
 $\eta = \frac{2 \ln 2}{3 \ln 2 + \frac{2}{\gamma - 1}}$.

51. Ans. : ACD

Sol. $W_{12} = \frac{1}{2} (P_0 + P_1) (V_2 - V_0)$
 $W_{12} - W_{13} < 0 \quad Q_{12} - Q_{13} = W_{12} - W_{13}.$

52. Ans. : ACD

Sol. $Q' = \text{Heat transfer rate} = 8\pi kr_0 T_0$

$$T_p = \frac{5T_0}{3}.$$

53. Ans. : C

54. Ans. : A

55. Ans. : B

Sols. At A $U = \frac{3nRT_A}{2} \quad \therefore T_A = 401.6 \text{ K}.$

As CA in $U - V$ graph passes through the origin $U \propto V \quad \therefore \text{CA is isobaric process.}$

$$W_{\text{cycle}} = nR(T_A - T_C) + nRT_A \ln 2$$

$$= -2058.4 \text{ J}$$

56. Ans. : B

57. Ans. : D

58. Ans. : D

Sols. $Q' = -KA \frac{dT}{dx} \quad \frac{Q'dx}{AK_0 \left(1 - \frac{x}{3a}\right)} = -dT.$

$$\frac{Q'}{AK_0} (-3a) \left[\ln \left(1 - \frac{x}{3a}\right) \right]_{-a}^{+a} = - \int_{T_1}^{T_2} dT$$

$$\frac{3Q'a}{AK_0} \ln(2) = T_1 - T_2$$

$$\frac{Q'}{AK_0} (-3a) \left[\ln \left(1 - \frac{x}{3a}\right) \right]_{-a}^0 = - \int_{T_1}^{T_0} dT = T_1 - T_0$$

$$- \frac{3Q'a}{AK_0} \left[0 - \ln \left(\frac{4}{3}\right) \right] = T_1 - T_0.$$

$$\therefore T_0 = T_1 - (\ln 4/3) (3Q'a/AK_0)$$

$$= T_1 - (\ln 4/3) (T_1 - T_2/\ln 2)$$

$$= T_1 - (T_1 - T_2) \frac{\ln 4 - \ln 3}{\ln 2}$$

$$= T_1 - (T_1 - T_2) \left(2 - \frac{\ln 3}{\ln 2} \right)$$

$$\frac{dT}{dx} = - \frac{Q'}{kA} = - \frac{Q'}{k_0 (\pi R^2)} = - \frac{(T_1 - T_2)}{3a \ln 2}$$

$$\frac{(T_1 - T_2) AK_0}{3a \ln 2} = \frac{K_{eq.} A (T_1 - T_2)}{2a}$$

$$\therefore K_{eq.} = K_0 \left(\frac{2}{3 \ln 2} \right)$$

59. Ans. : A - Q, B - PR, C - PS, D - PQ

Sol. For a process $PV^x = \text{constant}$ ($x \neq 1$)

$$\Delta V = nC_V(T_2 - T_1)$$

$$W_{12} = \frac{nR(T_1 - T_2)}{x-1}$$

$$Q_{12} = \frac{nR(T_2 - T_1)(x - \gamma)}{(x-1)(\gamma-1)}$$

Monoatomic gas $\gamma = 5/3$

The process is $TV^{x-1} = \text{constant}.$

When $x = \gamma \quad Q = 0$, when $x > 1$ and $< \gamma \quad x = 1.5$
 $Q < 0$

When $x < 1$ and $< \gamma \quad x = 0.75 \quad Q > 0$

60. Ans. : A - PQ, B - QR, C - PQ, D - PS

Sol. A : $PV^{-1} = \text{constant}; \quad B. : P\gamma^2 = \text{constant}$
 C. : $PV^{0.5} = \text{constant}; \quad D. : V = \text{constant.} \quad \gamma = 7/5.$