

Only **ONE** correct answer:

- If  $f(x) = \cos|x| + \left\lceil \frac{\sin x}{x} \right\rceil$  where  $\lceil \cdot \rceil$  denotes the G.I. function then  $f(x)$  is
  - even
  - odd
  - neither even nor odd
  - both even and odd simultaneously
- If  $f(x) = \sqrt{x-1}$ ,  $g(x) = -\ln x$ , the domain of  $\text{gof}(x)$  is:
  - $(0, 1/e)$
  - $(1, \infty)$
  - $(1, e)$
  - none
- $4\sin 50^\circ - \sqrt{3} \tan 50^\circ$  is equal to:
  - 0
  - 1
  - 2
  - none
- The range of  $\sin^{-1} x - \cos^{-1} x$  is
  - $[-3\pi/2, -\pi/2]$
  - $[-\pi/2, \pi/2]$
  - $[0, \pi]$
  - $[-3\pi/2, \pi/2]$
- Let  $f: \mathbb{R} \rightarrow [0, \pi/2)$  be a function defined by  $f(x) = \tan^{-1}(x^2 + x + a)$ . If  $f$  is onto then 'a' is equal to
  - 0
  - 1
  - $1/2$
  - $1/4$
- If  $f(x) = \begin{cases} [x] & x \geq 0 \\ 1 + [x] & x < 0 \text{ and } x \notin I \\ x & x < 0 \text{ and } x \in I \end{cases}$  then
  - $f(x)$  is periodic function
  - $f(x)$  is many one
  - $f(x)$  is one-one
  - none of these
- $y = \log_4 \log_2 \log_{1/2} x$ . The domain of this function is
  - $x \in (0, 1/2)$
  - $x \in [0, 1/2]$
  - $x \in (0, 1/2]$
  - $n \in [0, 1/2]$
- The domain of the function  $y = \log_{[x^2]}^{(4-x)}$  is where  $[\cdot]$  denotes G.I. function
  - $x \in [\sqrt{2}, 4]$
  - $x \in (1, \infty)$
  - $x \in (0, \infty)$
  - $\mathbb{R} - \{0, 1\}$
- The domain of the function  $y = \sqrt{\sin^{-1}(\log_2^x)}$  is
  - $[1, 2]$
  - $(1, 2)$
  - $x > 0, x \neq 1$
  - $x > 1$
- $\text{cosec} \frac{2\pi}{7} + \text{cosec} \frac{4\pi}{7} + \text{cosec} \frac{8\pi}{7}$  is equal to:
  - 0
  - 1
  - 2
  - none
- Let  $f(x) = \frac{3^{1+\ln x}}{x^{\ln 3}}$ . Then  $f(1993)$  is
  - 3
  - 4
  - 5
  - 6
- If  $\cos \alpha + \cos \beta = \cos(3\pi/7)$ ,  $\sin \alpha + \sin \beta = \sin(3\pi/7)$  then  $\sin^2(\alpha-\beta)/2$  is equal to:
  - $1/4$
  - $3/4$
  - $-3/4$
  - $-1/4$
- $\text{cosec} 10^\circ - 4\sin 70^\circ$  is equal to:
  - 0
  - 1
  - 2
  - 3
- If  $\sin^4 x + \sin^2 x = 1$  then  $\tan^4 x - \tan^2 x$  is:
  - 0
  - 1
  - 2
  - none
- In a right angled  $\Delta$ , the hypotenuse is four times as long as perpendicular drawn to it from the opposite vertex. One of the acute angle is:
  - $15^\circ$
  - $30^\circ$
  - $45^\circ$
  - $60^\circ$
- In  $\Delta ABC$ ,  $\frac{r_1 + r_2}{1 + \cos c}$  is equals to:
  - $\frac{2\Delta}{abc}$
  - $\frac{2abc}{\Delta}$
  - $\frac{abc}{2\Delta}$
  - $\frac{abc}{\Delta^2}$
- If twice the square of the diameter of a circle is equal to half the sum of squares of the sides of inscribed  $\Delta ABC$ , then  $\sin^2 A + \sin^2 B + \sin^2 C =$ 
  - 1
  - 2
  - 4
  - 8
- Show that  $f: [-2\pi, 2\pi] \rightarrow \mathbb{R}$  defined by  $f(x) = \frac{\cos x}{[x/5\pi] + 0.5}$  where  $[\cdot]$  step function is odd function.
- If  $f(a-x) = f(a+x)$  and  $f(b-x) = f(b+x)$  where  $a$  and  $b$  are real numbers and  $a > b$ , show that  $f$  is periodic and find its period
- If  $f$  is a one-one odd function, find  $x$  for which  $f(x) + f\left(\frac{x-4}{x+2}\right) = 0$ .
- If  $\cos A + \cos B - \cos(A+B) = 3/2$  and  $A$  and  $B$  are acute, find  $A$  and  $B$ .
- Solve for  $x$  and  $y$ :  $\cos y \sqrt{\sin x} = 0$  and  $2\sin^2 x - \cos 2y - 2 = 0$ ,
- Solve:  $\sin^2 4x + \cos^2 x = 2\sin 4x \cos^4 x$ .